

# Assessing Progress in SAT Solvers Through the Lens of Incremental SAT

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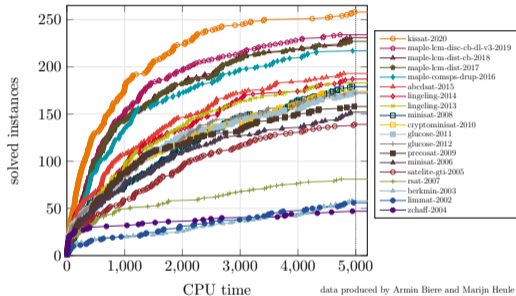
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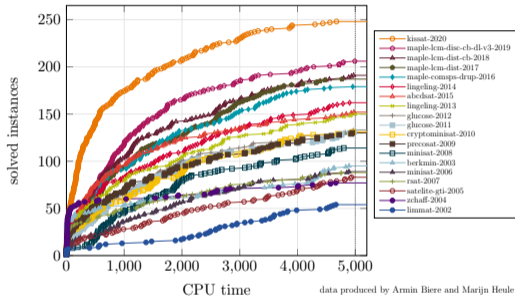
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SAT2021

SAT Competition Winners on the SC2019 Benchmark Suite



SAT Competition Winners on the SC2020 Benchmark Suite

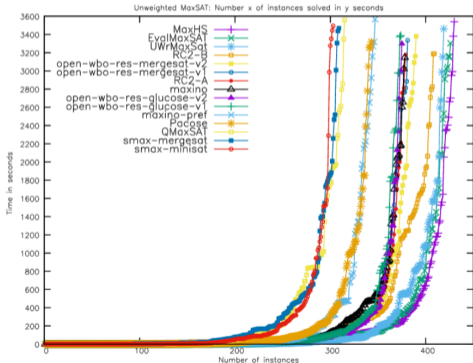


- The winners of recent SAT Competitions achieved a great progress during the last several years<sup>1</sup>.

<sup>1</sup>The plots are courtesy of Armin Biere (<http://fmv.jku.at/kissat/>)

- Nevertheless many applications which employ incremental SAT solvers (e.g. MaxSAT solvers) prefer to use the good old MiniSAT 2.2 (2008) or Glucose 3 (2013)/ Glucose 4 (2014).
  - Example: MaxSAT Evaluation 2020 participants <sup>2</sup>:

Algorithm	Backend
UWrMaxSAT	CoMiniSATPS
MaxHS smax	MiniSat 2.2
open-wbo-v1,v2 smax	MergeSAT
RC2-B,A open-wbo-v1,v2 maxino, maxino-pref Pacose QMaxSAT	Glucose



<sup>2</sup><https://maxsat-evaluations.github.io/2020/>

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  - Minimum unsatisfiable subset (MUS) extraction.
- Compare its performance with that of MiniSAT / Glucose.



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- **2020. SLS.** Relaxed\_LCMDCBDL\_newTech incorporated into the solver a stochastic local search component, complemented with *rephasing* technique and a novel approach to bumping activity values in CDCL component based on some of the statistics accumulated by the SLS component.

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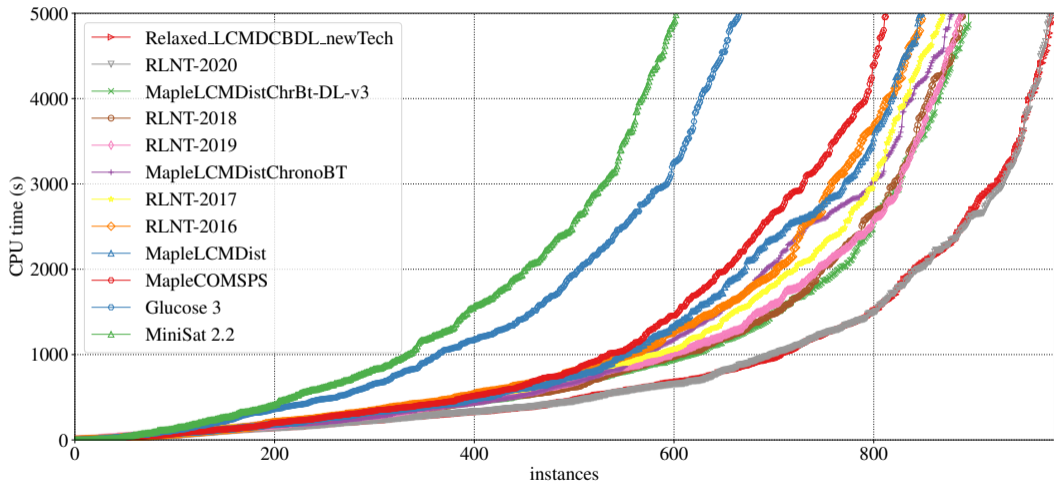
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## RLNT

It was decided to develop a single solver based on Relaxed\_LCMDCBDL\_newTech, such that the modern heuristics can be separately disabled and enabled. The solver was called RLNT.

With all heuristics enabled it differs from Relaxed\_LCMDCBDL\_newTech in the support of the incremental mode and in several small fixes.

- RLNT-2020 – RLNT with DIST, LCM, CB, DL, SLS.
- RLNT-2019 – RLNT with DIST, LCM, CB, DL.
- RLNT-2018 – RLNT with DIST, LCM, CB.
- RLNT-2017 – RLNT with DIST, LCM.
- RLNT-2016 – RLNT without any of heuristics enabled.
- Relaxed\_LCMDCBDL\_newTech – SAT Competition 2020 2nd place.
- MapleLCMDistChronoBT-DL-v3 – SAT Race 2019 winner.
- MapleLCMDistChronoBT – SAT Competition 2018 winner.
- MapleLCMDist – SAT Competition 2017 winner.
- MapleCOMSPS – SAT Competition 2016 winner.
- Glucose 3.0.
- MiniSat 2.2.

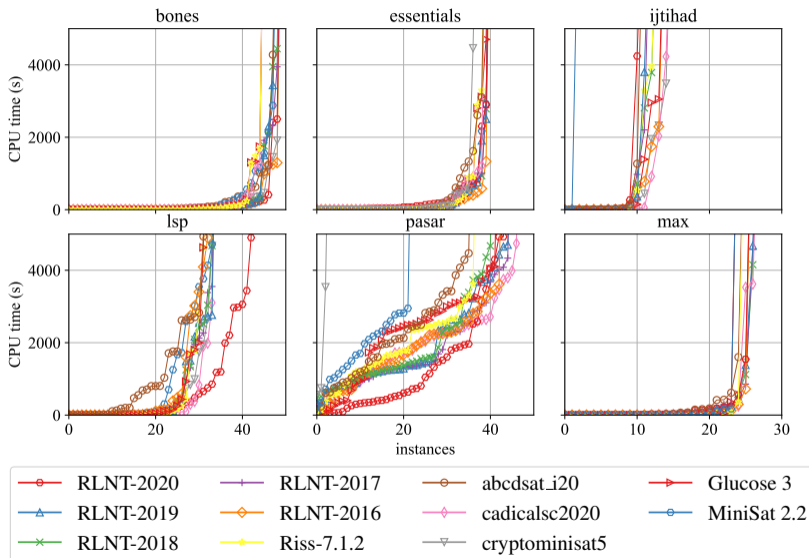


Incremental track 2020 included the following applications:

- *bones*: finding backbones of a CNF SAT formula
- *essentials*: finding variables essential for the satisfiability of a formula
- *lsp*: finding the longest simple path in a graph
- *max*: a simple MaxSAT solver
- *ijtihad*: QBF solver
- *pasar*: planning solver

For each application, there were 50 benchmarks (*bones* and *essentials* used the same set of benchmarks), i.e. 250 benchmarks in total.

# Evaluation of considered solvers in Incremental Track 2020: Cactus plots



	<i>bones</i>		<i>essentials</i>		<i>lsp</i>		<i>max</i>		<i>ijtihad</i>		<i>pasar</i>	
	S	P2	S	P2	S	P2	S	P2	S	P2	S	P2
RLNT-2020	49	350	40	2219	<b>43</b>	<b>1987</b>	26	4869	11	6879	44	2325
RLNT-2019	48	580	40	2170	34	3546	27	4753	12	6845	45	2733
RLNT-2018	49	482	40	2168	34	3577	<b>27</b>	<b>4739</b>	13	6393	41	3254
RLNT-2017	49	441	40	2174	34	3542	27	4745	12	6845	45	2553
RLNT-2016	<b>49</b>	<b>322</b>	<b>40</b>	<b>2086</b>	33	3837	26	4826	14	6369	43	2902
Glucose 3	45	1108	40	2273	32	3845	24	5211	14	6895	42	3387
MiniSat 2.2	48	635	40	2180	34	3811	24	5212	2	9600	22	6380
Riss-7.1.2	45	1108	39	2388	32	3844	25	5013	13	7270	37	3907
abcsat_i20	48	627	39	2450	32	4205	25	4696	11	7830	36	4295
cadicalsc2020	45	1085	39	2323	34	3381	27	4756	15	6729	<b>47</b>	<b>2400</b>
cryptoMiniSat5	49	333	37	2737	34	3495	26	4478	<b>15</b>	<b>5966</b>	3	9496

- It is clear that RLNT configurations are on par or better than competition (see *lsp* column).
- Contrary to what is observed on main track benchmarks, the difference between modern solvers and MiniSAT/ Glucose becomes much less pronounced.



Next we use the 5 developed RLNT configurations (2016-2020) in two concrete practical settings where incremental calls to a SAT oracle are of crucial importance: *Maximum Satisfiability (MaxSAT) solving* and *Minimal unsatisfiable subset (MUS) extraction*, and compare them with Glucose 3 and MiniSAT 2.2.

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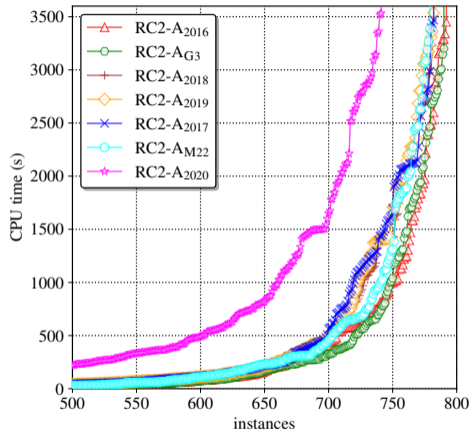
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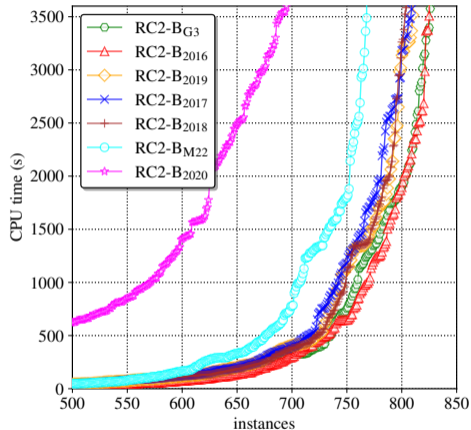
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  - *mostly unsatisfiable oracle calls*
- Linear search SAT-UNSAT algorithm for MaxSAT (*LSU*)
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- A simple deletion-based MUS extractor (*MUS<sub>x</sub>*).
  - *mixed (satisfiable and unsatisfiable) oracle calls*

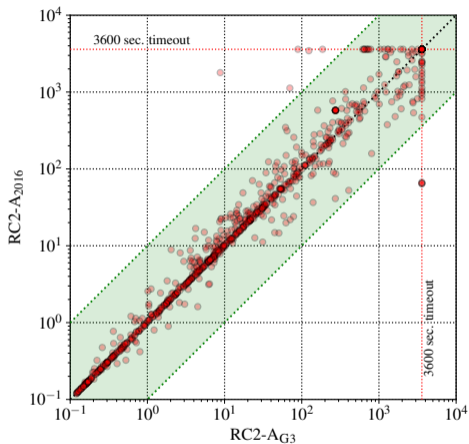
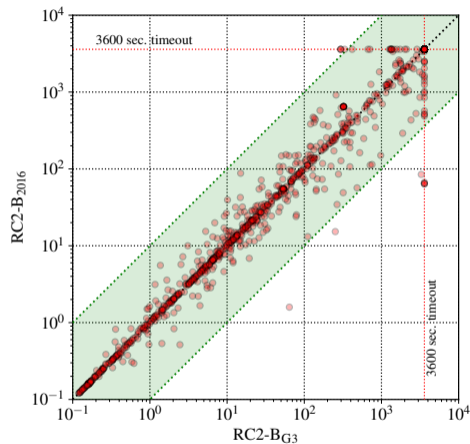
- The RC2 MaxSAT solver belongs to the large family of core-guided MaxSAT solvers and provides an efficient implementation of the OLL/RC2 algorithm.
- Each iteration performed by the solver involves calling a SAT oracle incrementally given an unsatisfiable formula that is slightly modified at each iteration.
- The solver proceeds until the final iteration, which determines the working formula to be satisfiable.
- The solver can also be instructed to apply a few additional heuristics, some of which may increase the number of satisfiable oracle calls; however, unsatisfiable oracle calls still prevail.
- The competition configurations RC2-A and RC2-B make use of the Glucose 3 SAT solver.
- This part of the experiment tested RC2 on the complete set of benchmarks (both unweighted and weighted) from the MSE'20.



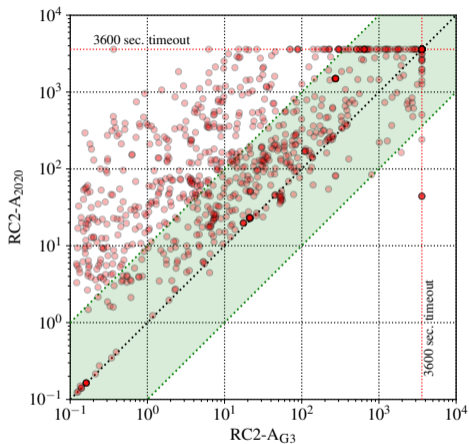
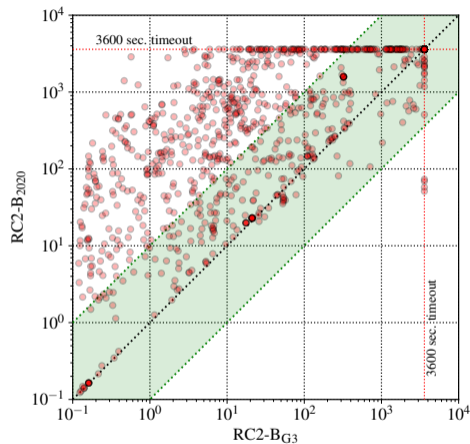
Performance of RC2-A



Performance of RC2-B

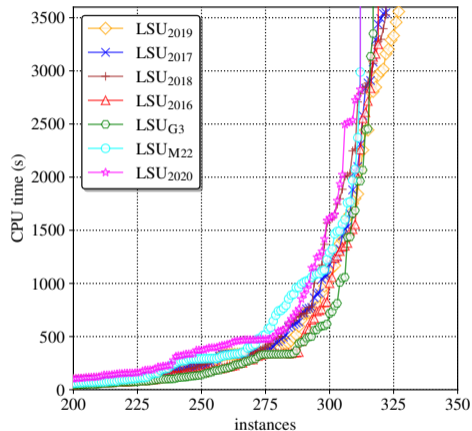
RC2-A<sub>G3</sub> vs RC2-A<sub>2016</sub> (best)RC2-B<sub>G3</sub> vs RC2-B<sub>2016</sub> (best)



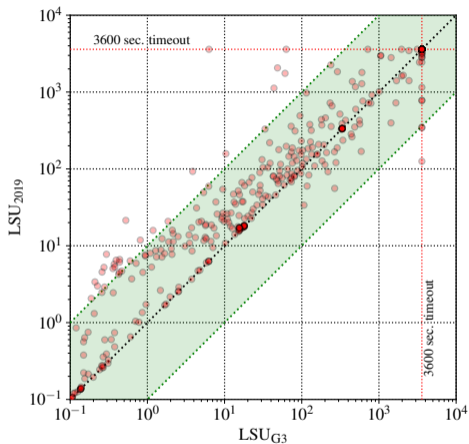
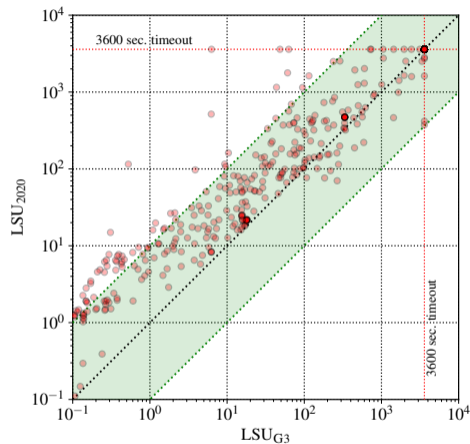
RC2-A<sub>G3</sub> vs RC2-A<sub>2020</sub> (worst)RC2-B<sub>G3</sub> vs RC2-B<sub>2020</sub> (worst)

- The LSU MaxSAT algorithm performs a linear search iterating over the possible numbers of satisfied soft clauses.
- It decreases this number as long as the underlying solver reports the current formula to be satisfiable.
- Thus, all but one iterations of the algorithm involve satisfiable oracle calls.

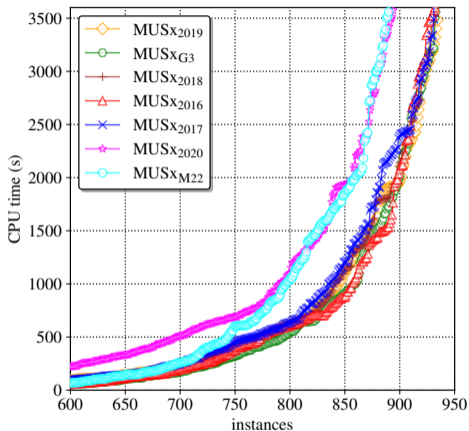
**Note.** Evaluation was made only using un-weighted formulas.



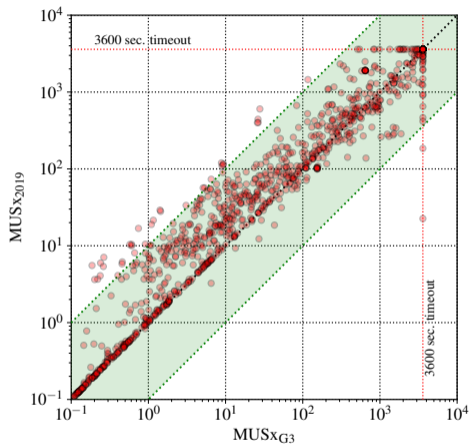
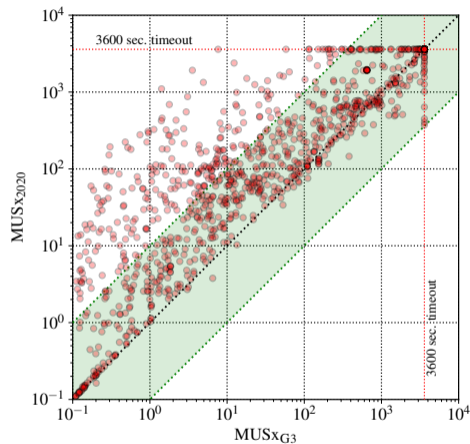
Performance of LSU


 $LSU_{G3}$  vs  $LSU_{2019}$  (best)

 $LSU_{G3}$  vs  $LSU_{2020}$  (worst)

- MUSx implements the simple deletion-based algorithm, which is bootstrapped with an unsatisfiable core of a formula.
- It iterates over all clauses of the core trying to incrementally get rid of them one-by-one to get an MUS, so the outcomes of incremental SAT solver calls are mixed.
- We generated a large collection of new MUS benchmarks based on the MSE'20 benchmark set (1103 formulas in total).
- To ensure that the reduction phase computes exactly the same MUS, for each benchmark MUSx was bootstrapped with an initial unsatisfiable core, which was always obtained by Glucose 3.



Performance of MUSx

MUS<sub>xG3</sub> vs MUS<sub>x2019</sub> (best)MUS<sub>xG3</sub> vs MUS<sub>x2020</sub> (worst)

	MiniSat 2.2	Glucose 3	RLNT-2016	RLNT-2017	RLNT-2018	RLNT-2019	RLNT-2020
RC2-A	2536.8	2466.3	<b>2462.5</b>	2544.6	2536.7	2543.9	2875.7
RC2-B	2628.1	2287.7	<b>2281.3</b>	2406.0	2406.1	2387.5	3272.8
LSU	3391.1	3307.4	3302.7	3306.3	3318.7	<b>3259.7</b>	3411.7
MUSx	1621.4	<b>1333.9</b>	1345.7	1386.3	1361.8	1353.8	1665.7
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- There is a need for discussion in the SAT community to bridge the gap between practical applications of SAT solvers and the SAT Competition.

Thank you for your attention!